

# The relationship between FRQ-protein stability and temperature compensation in the *Neurospora* circadian clock

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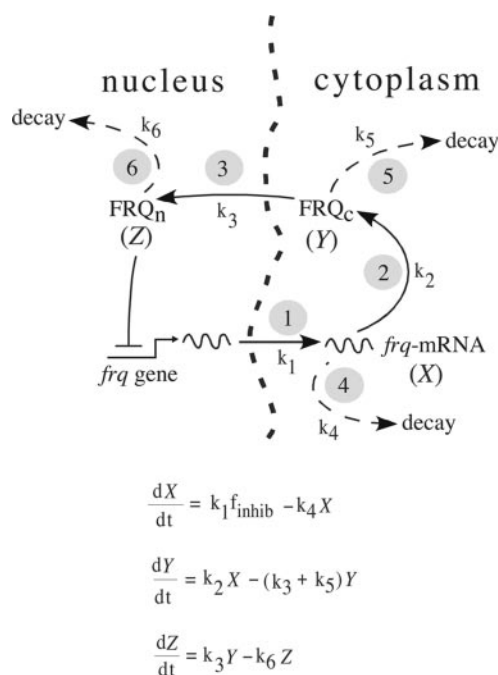
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Temperature compensation is an important property of all biological clocks. In *Neurospora crassa*, negative-feedback regulation on the *frequency* (*frq*) gene's transcription by the FRQ protein plays a central role in the organism's circadian pacemaker. Earlier model calculations predicted that the stability of FRQ should determine the period length of *Neurospora*'s circadian rhythm as well as the rhythm's temperature compensation. Here, we report experimental FRQ protein stabilities in *frq* mutants at 20°C and 25°C, and estimates of overall activation energies for mutant FRQ protein degradation. The results are consistent with earlier model predictions, i.e., temperature compensation of *Neurospora*'s circadian rhythm is a highly regulated process where the stability of FRQ is an important factor in determining *Neurospora*'s circadian period as well as the clock's temperature compensation. The partial loss of temperature compensation in *frq*<sup>7</sup> and *frq*<sup>55131</sup> mutants can be described by a simple negative-feedback model (the Goodwin oscillator) when the experimentally obtained activation energies of FRQ degradation for these mutants are incorporated into the model.

FREQUENCY protein

Circadian clocks are physiological oscillators, which are important in the daily and seasonal adaptation of organisms to their environment (1–4). A characteristic property of circadian clocks is the ability to keep the period length approximately constant despite changes in ambient environmental conditions (5). Temperature compensation, the approximate constancy of the period at different constant temperatures, is one of the best known examples of circadian period homeostasis. Despite the relative insensitivity of the circadian period to temperature, the underlying physiological component processes are generally quite dependent on temperature, with  $Q_{10}$  values of 2 or even higher. The mechanisms behind temperature compensation are not well understood, although a general theory applicable to reaction kinetic oscillator models (6–22) can be formulated (23–28).

In the model organism *Neurospora crassa*, the *frequency* (*frq*) gene has a central role in generating a circadian conidiation rhythm by means of a transcriptional and translational negative-feedback loop (29–32). This negative-feedback loop is considered to be part of a central oscillator that controls a variety of rhythmic output genes, so-called clock-controlled genes (30, 31). We have taken the negative-feedback loop in its simplest manifestation [Fig. 1 Upper (compare with refs. 30 and 31)] and cast it as a Goodwin-type model [Fig. 1 Lower (33)]. As implemented, the model assumes that kinetically important rate constants involve the transcription yielding *frq* mRNA, its translation, and the net nuclear import of FRQ, as well as the decay of these species. Events associated with the processing of *frq* primary transcripts, their export to the cytoplasm, and their assembly onto ribosomes are subsumed under rate 1, and as a first approximation, the impact of FRQ in inhibiting its own gene's expression is taken to be an immediate function of its nuclear concentration. Despite these approximations, simulation calculations with the Goodwin model showed that the dynamics of the *frq*



**Fig. 1.** The model. (Upper) Negative-feedback loop of the *Neurospora* circadian clock (30, 31). Encircled numbers ("i") correspond to processes  $R_i$  with rate constants  $k_i$ : 1, export of primary *frq* transcript into cytoplasm and assembly onto ribosomes; 2, translation to FRQ protein; 3, import of cytosolic FRQ into nucleus; 4, degradation of transcript; 5 and 6, degradation of cytosolic and nuclear forms of FRQ, respectively. (Lower) Goodwin-type equations that were used in the calculations. The variables are  $X = \text{frq-mRNA}$ ,  $Y = \text{FRQ}_c$  (cytosolic FRQ), and  $Z = \text{FRQ}_n$  (nuclear FRQ). For rate-constant values and initial concentrations, see Table 1.

negative-feedback loop are in good agreement with experimental phase-resetting kinetics (16, 17, 34, 35). The model's predictions were that the stability of the FRQ protein not only should have a major influence on the clock's period length but that a regulated thermal stability of FRQ is required to maintain temperature compensation (35, 36). These predictions were partly confirmed by experiments, where the stability of the FRQ protein was altered by replacing the phosphorylation site serine 513 by isoleucine (37). These results were supported by another study where a PEST-like sequence was removed from FRQ (38), which also resulted in a more stable FRQ-protein (compared with *frq*<sup>+</sup>) and an increased period length.

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Guided by the model predictions, the aim of this study was to obtain estimates for the thermal stability of FRQ in *frq* mutants by measuring the overall activation energies of FRQ degradation and correlating the stability data with the mutant rhythms' temperature sensitivities. The results show that the partial loss of temperature compensation in *frq*<sup>7</sup> and *frq*<sup>S5131</sup> mutants is related to an increase in FRQ's stability (causing a larger period length) and an increase in the activation energy of FRQ degradation (causing a more temperature-sensitive period). By incorporating the experimentally determined activation energies of FRQ degradation into the Goodwin model (Fig. 1), we were able to consistently describe the periods and the occurrence/loss of temperature compensation in *frq*<sup>+</sup>, *frq*<sup>1</sup>, *frq*<sup>7</sup>, and *frq*<sup>S5131</sup> mutants.

## A Theory of Temperature Compensation

When describing the time evolution of a physiological system by reaction kinetics, the system is broken down into a set of component reactions  $R_i$ , which are translated into chemical rate equations (39). The influence of temperature on an individual process  $R_i$  is described by the Arrhenius equation (Eq. 1)

$$k_i = A_i e^{-\frac{E_i}{RT}}, \quad [1]$$

where  $k_i$  is the rate constant of process  $R_i$ . Symbols  $E_i$ ,  $R$ ,  $T$ , and  $A_i$  denote the activation energy, gas constant, temperature, and collision factor, respectively (40). The activation energy,  $E_i$ , is a measure of how sensitive process  $R_i$  is toward variations in temperature.

For a chemical/metabolic oscillator, the period  $P$  depends on the individual processes  $R_i$  and their corresponding rate constants  $k_i$ , i.e.,

$$P = P(k_1, k_2, \dots, k_i, \dots, k_N). \quad [2]$$

Temperature compensation requires that the period  $P$  is independent of temperature, which leads to the condition (see Appendix):

$$\frac{d \ln P}{dT} = \frac{1}{RT^2} \sum_{i=1}^N C_i^P E_i = 0, \quad [3]$$

where the  $C_i^P$  (control coefficients) obey the summation theorem (41, 42):

$$\sum_{i=1}^N C_i^P = -1. \quad [4]$$

Because activation energies  $E_i$  are positive, Eq. 3 requires that the  $C_i^P$  must have positive and negative values. This is equivalent to the presence of an "antagonistic balance" of opposing reactions (23) that resemble the compensation mechanisms in mechanical and electronic clocks (27). In fact, almost 50 years ago, Hastings and Sweeney (43) suggested that opposing reactions may lead to temperature compensation in circadian rhythms. Interestingly, for physicochemical oscillators, the presence of positive and negative  $C_i^P$  values appears to be closely related to the presence of positive- and negative-feedback loops as a necessary part of the rhythm generator (23, 44). We are not aware of any reaction kinetic oscillator model that has only negative  $C_i^P$  values (note that such an oscillator could not have temperature compensation). Thus, any reaction kinetic oscillator should in principle be able to show temperature compensation when suitable activation energy combinations (Eq. 3) are chosen.

By integrating Eq. 3, and assuming that  $\sum_i C_i^P E_i$  is temperature independent, the following expression for  $P$  can be obtained:

**Table 1. Rate constants, control coefficients, and activation energies used in the model calculations**

Reaction i	Rate constant $k_i$ , h <sup>-1</sup>	$C_i^P$ (15% variation of the $k_i$ s)	$E_i$ , kJ/mol	$C_i^P E_i$ , kJ/mol
1	0.3	0.131	190	24.9
2	0.3	0.093	190	17.7
3	0.3	-0.040	190	-7.6
4	0.27	-0.470	30	-14.1
5	0.2*	-0.131	30 <sup>†</sup>	-3.9
6	0.2*	-0.628	30 <sup>†</sup>	-18.8
$\sum_i C_i^P = -1.045$			$\sum_i C_i^P E_i = -1.8$	

The given rate constant values are defined for  $T_{\text{ref}} = 292$  K. Rate constants  $k_5$  and  $k_6$  (with asterisk) differ for the various *frq* mutants. Initial concentrations (a.u.) used in all calculations:  $X = 6.124 \times 10^{-2}$ ,  $Y = 8.452 \times 10^{-2}$ ,  $Z = 5.245 \times 10^{-1}$ . Threshold for *frq* transcription inhibition,  $Z_{\text{max}} = 0.1$  a.u.; threshold for reactivating *frq* transcription,  $Z_{\text{min}} = 0.05$  a.u. (used in all calculations).

\* $k_5$ ,  $k_6$  values for *frq*<sup>+</sup> at  $T_{\text{ref}} = 292$  K. The following  $k_5$ ,  $k_6$  values (defined at  $T_{\text{ref}} = 292$  K) have been used in the calculations for the other mutants: *frq*<sup>1</sup>, 0.320 h<sup>-1</sup>; *frq*<sup>7</sup>, 0.124 h<sup>-1</sup>; *frq*<sup>S5131</sup>, 0.080 h<sup>-1</sup>.

<sup>†</sup> $E_5$  and  $E_6$  values for *frq*<sup>+</sup>. The following  $E_5$ ,  $E_6$  values ( $E_5 = E_6$ ) have been used in the calculations for the other mutants (see also Table 2): *frq*<sup>1</sup>, 29 kJ/mol; *frq*<sup>7</sup>, 46 kJ/mol; *frq*<sup>S5131</sup>, 59 kJ/mol.

$$P = C \exp\left(-\sum_i C_i^P E_i / RT\right), \quad [5]$$

where  $C$  is a constant (see Appendix).

Once the rate constants are defined for a given reference temperature,  $T_{\text{ref}}$ , concentrations and the control coefficients can be calculated for a given temperature,  $T$ .

Table 1 shows the *frq*<sup>+</sup> rate constants used and the model's  $C_i^P$  values. Slight modifications of the present model compared with the earlier version (34) include thresholds for inhibition and start of *frq* transcription, respectively (Table 1). This allows for an extended parameter space for which oscillations can be observed (35). The different *frq* mutants are represented in the model by different values for the FRQ degradation rate constants  $k_5$ ,  $k_6$  and activation energies  $E_5$ ,  $E_6$ . Because in the experiments total FRQ (i.e., cytosolic and nuclear FRQ) is measured, and for the sake of simplicity, we assumed that  $k_5 = k_6$  and  $E_5 = E_6$  (Table 1).

The negative control coefficients  $C_5^P$ ,  $C_6^P$  (Table 1) indicate that when temperature compensation in the model is lost because of increased  $E_5$ ,  $E_6$  values (leading to decreased  $k_5$ ,  $k_6$  values), the period should decrease with increasing temperature leading (as in the *frq*<sup>7</sup> mutant) to negative  $d \ln P / dT$  values (Eq. 3). Although experimental results with the *frq*<sup>S5131</sup> and *frq*<sup>ΔPEST-1</sup> mutants (37, 38) indeed confirmed that a more stable FRQ protein leads to larger period lengths, the question of which properties of FRQ relate to changes in temperature compensation were so far not considered. Here, we show that variations in the overall experimental activation energies of FRQ degradation are consistent with the dynamics of a Goodwin oscillator and can account for the various degrees of temperature compensation in the *frq* mutant alleles.

## Materials and Methods

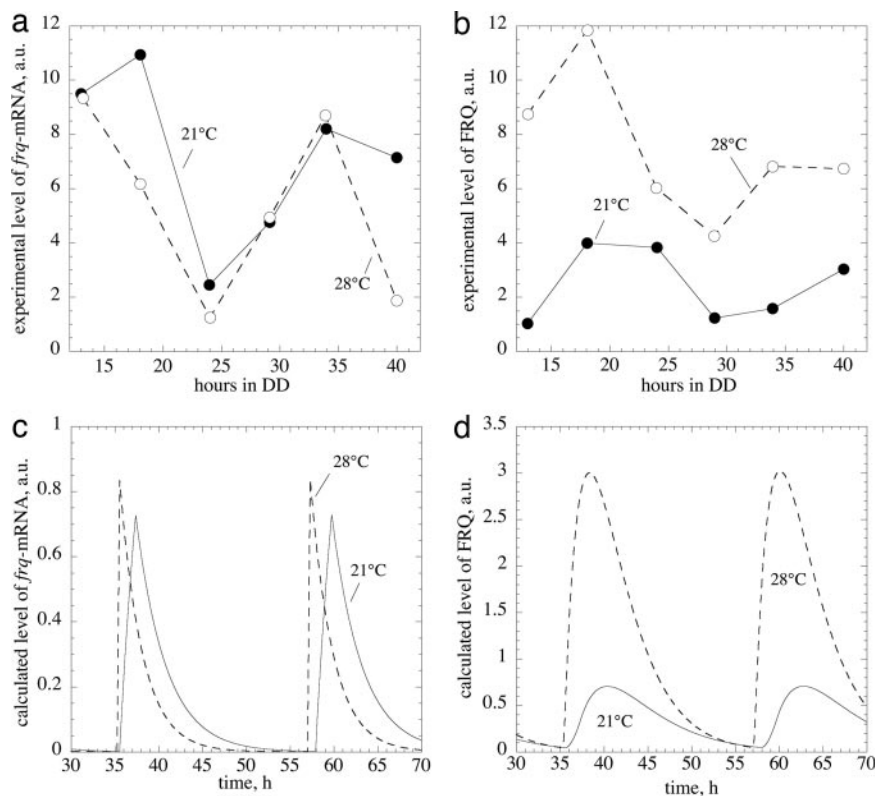
**Model Calculations.** The model calculations with the Goodwin oscillator (Fig. 1 and Table 1) were done by using the FORTRAN subroutine LSODE (Livermore Solver of Ordinary Differential Equations) (45).

**Growth-Tube Experiments.** Growth tubes were prepared as described in ref. 46 with 1× Vogel's medium, 0.2% glucose, 0.17% arginine, and 1.5% agar. The tubes were inoculated with conidia and transferred to incubators (darkness) directly after inoculation at different but constant temperatures ( $\pm 0.5^\circ\text{C}$ ). Measuring the distance between two distant conidiation peaks and dividing the









**Fig. 5.** Temperature behavior of *frq*<sup>+</sup>-mRNA and FRQ<sup>+</sup> amplitudes. *a* and *b* show earlier experimentally determined *frq*<sup>+</sup>-mRNA and FRQ<sup>+</sup> levels measured at 21°C (solid lines) and 28°C (dashed lines). The data are replotted from Liu *et al.* (51). *c* and *d* show calculated concentration profiles of *frq*<sup>+</sup>-mRNA and FRQ<sup>+</sup> protein in the temperature compensated Goodwin model (Fig. 1 and Table 1) at 21°C (solid lines) and 28°C (dashed lines). Because in the experiment (*b*) total (i.e., nuclear and cytosolic) FRQ was measured, calculated FRQ levels are represented by the sum of variables *Y* (cytosolic form of FRQ) and *Z* (nuclear form of FRQ; see Fig. 1).

sudden change of certain properties within the balancing process, which can no longer be maintained at higher temperatures. Interestingly, this strong temperature dependence of *Neurospora*'s period length above 30°C resembles closely what is observed for most chemical oscillatory reactions (see discussion below).

There exist strains of *Neurospora* that affect temperature compensation by mutations in genes other than *frq*. In particular, *prd-4* has a short period but is defective in temperature compensation by decreasing its period with increasing temperature (52). Our model suggests that *prd-4* should have an increased FRQ turnover compared with *prd-4<sup>+</sup>*, leading to shorter period lengths. In addition, the activation energy of FRQ degradation should also be increased in *prd-4*, leading to a negative balance equation,  $\sum_i c_i^p E_i < 0$ , and resulting in decreasing periods with increasing temperature. PRD-4 is a cell cycle kinase that, when mutated, leads to premature phosphorylation of FRQ (A. Pregueiro, J.C.D., and J.J.L., unpublished work) and possibly to an increased degradation rate of FRQ.

Temperature compensation likely emerged through an evolutionary process with the adaptation of reaction sensitivities and activation energies such that  $\sum_i C_i^p E_i \approx 0$ . FRQ is a central clock element, and its stability is highly regulated through a variety of means including PEST-like sequences and multiple phosphorylation sites, which are part of *Neurospora*'s temperature-compensation mechanism. Both CKII and CAMK-1 along with the phosphatase PP1 have been identified as determining FRQ's stability and being essential for the normal operation of *Neurospora*'s circadian clock (53–56). There is also evidence that FRQ degradation requires FWD1, an F-box/WD-40 repeat-containing protein, which is considered to be necessary for the ubiquitination of FRQ and its degradation via the ubiquitin-proteasome pathway

(50). More indirectly, FRQ turnover is also regulated by the COP9 signalosome that controls the FWD1 ubiquitin ligase complex (57).

Contrary to the evidence presented above that temperature compensation in *Neurospora*'s circadian clock is a highly regulated process, the majority of chemical oscillators depend rather heavily on temperature. In these oscillators, the frequency generally obeys Van't Hoff's rule with  $Q_{10}$  values of  $\approx 2$ –3. Because in chemical oscillators component processes are “evolutionary unrelated,” one can assume that component processes obey Van't Hoff's rule with  $Q_{10}$  values of 2–3. At 25°C, this would correspond to an average activation energy,  $\langle E_a \rangle$ , of the frequency of  $\approx 50$ –85 kJ/mol. By making this assumption and replacing the  $E_i$  in Eq. 3 by  $\langle E_a \rangle$ , the balance equation reduces with help of Eq. 4 to

$$\sum_i C_i^P \mathbf{E}_i = \sum_i C_i^P \langle E_a \rangle = \langle E_a \rangle \sum_i C_i^P = -\langle E_a \rangle, \quad [9]$$

which, when inserted into Eq. 5, leads to

$$P = Ce^{+\frac{\langle E_a \rangle}{RT}} \Leftrightarrow v = \frac{1}{C} e^{-\frac{\langle E_a \rangle}{RT}}, \quad [10]$$

showing why the periods  $P$  (or frequencies  $\nu$ ) depend exponentially on temperature with  $\langle E_a \rangle$  values between 50 and 85 kJ/mol. For example, in the Belousov–Zhabotinsky reaction, which is one of the most studied chemical oscillators (58), the period follows Eq. 10 over a large temperature range, indicating that  $\sum_i C_i^p E_i$  is approximately independent of temperature (59). As seen in Fig. 3b, this is also the case for the various *frq* mutants, at least for the temperature window in which temperature compensation is generally observed.

The data in Fig. 4 show that there is a correspondence between period length and FRQ half-life. However, it should be noted that this correspondence is temperature-dependent because, depending on the temperature, different period lengths can be observed for the same FRQ half-life.

Despite its simplicity, the Goodwin oscillator has previously been shown to simulate many circadian clock properties (16, 17, 34, 36). The temperature-compensated model presented here is able to provide a consistent, almost quantitative description of the temperature dependence of *frq*-mRNA and FRQ amplitudes and its period length, thereby showing that temperature compensation in the *Neurospora* circadian clock can be understood as part of the FRQ negative-feedback loop and pointing to a central role for FRQ. Many of the processes described by the equations in Fig. 1 are formulated as first-order reactions but are clearly more complex—as, for example, the degradation of FRQ, which appears to be degraded by the ubiquitin-proteasome pathway (50). As more detailed quantitative experimental data on various component processes become available, an amplified version of the model will be required to do quantitative simulations.

The approach taken here, i.e., combining experiments with theoretic principles and model calculations, appears to be useful for developing a quantitative picture of the regulatory elements, including temperature compensation, within the clockwork of circadian rhythms (27).

## Appendix

**Derivation of Eq. 3.** Applying the chain rule on Eq. 3 leads to

$$\frac{\partial P}{\partial T} = \sum_i \left( \frac{\partial P}{\partial k_i} \right) \left( \frac{\partial k_i}{\partial T} \right). \quad [11]$$

The last term in Eq. 11 can be explicitly calculated from the Arrhenius equation (Eq. 1), which gives

$$\frac{\partial P}{\partial T} = \sum_i \left( \frac{\partial P}{\partial k_i} \right) \frac{E_i}{RT^2} k_i = \sum_i \left( \frac{\partial P}{\partial \ln k_i} \right) \frac{E_i}{RT^2}. \quad [12]$$

Multiplying Eq. 12 by  $1/P$  and observing that  $\partial P/P = \partial \ln P$ , Eq. 12 can be written as

$$\frac{1}{P} \frac{\partial P}{\partial T} = \frac{\partial \ln P}{\partial T} = \frac{1}{RT^2} \sum_i \left( \frac{\partial \ln P}{\partial \ln k_i} \right) E_i = \frac{1}{RT^2} \sum_i C_i^P E_i. \quad [13]$$

**Derivation of Eq. 5.** Making the assumption that  $\sum_i C_i^P E_i$  is independent of temperature, Eq. 13 can be integrated

$$\int_{P_0}^P d \ln P' = \sum_i C_i^P E_i \int_{T_0}^T \frac{dT}{RT^2}, \quad [14]$$

leading to

$$P = P_0 e^{\frac{\sum_i C_i^P E_i}{-RT_0}} \times e^{-\frac{\sum_i C_i^P E_i}{-RT}} = C \times e^{-\frac{\sum_i C_i^P E_i}{-RT}}. \quad [15]$$

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- Dunlap, J. C. (1999) *Cell* **96**, 271–290.
- Bünning, E. (1963) *The Physiological Clock* (Springer, Berlin).
- Edmunds, L. N. (1988) *Cellular and Molecular Bases of Biological Clocks* (Springer, New York).
- Dunlap, J. C., Loros, J. J. & DeCoursey, P. J. (2003) *Chronobiology: Biological Timekeeping* (Sinauer Associates, Sunderland, MA).
- Pittendrigh, C. S. & Caldarola, P. C. (1973) *Proc. Natl. Acad. Sci. USA* **70**, 2697–2701.
- Forger, D. B. & Peskin, C. S. (2005) *Proc. Natl. Acad. Sci. USA* **102**, 321–324.
- Forger, D. B. & Peskin, C. S. (2003) *Proc. Natl. Acad. Sci. USA* **100**, 14806–14811.
- Goldbeter, A. (2002) *Nature* **420**, 238–245.
- Goldbeter, A. (1996) *Biochemical Oscillations and Cellular Rhythms: The Molecular Bases of Periodic and Chaotic Behavior* (Cambridge Univ. Press, Cambridge, U.K.).
- Gonze, D., Leloup, J. C. & Goldbeter, A. (2000) *C. R. Acad. Sci. Ser. III* **323**, 57–67.
- Kurosawa, G., Mochizuki, A. & Iwasa, Y. (2002) *J. Theor. Biol.* **216**, 193–208.
- Leloup, J. C. & Goldbeter, A. (2003) *Proc. Natl. Acad. Sci. USA* **100**, 7051–7056.
- Lüttge, U. (2000) *Planta* **211**, 761–769.
- Neff, R., Blasius, B., Beck, F. & Lüttge, U. (1998) *J. Membr. Biol.* **165**, 37–43.
- Murray, J. D. (1993) *Mathematical Biology* (Springer, Berlin).
- Ruoff, P., Vinsjevik, M., Mohsenzadeh, S. & Rensing, L. (1999) *J. Theor. Biol.* **196**, 483–494.
- Ruoff, P., Vinsjevik, M., Monnerjahn, C. & Rensing, L. (2001) *J. Theor. Biol.* **209**, 29–42.
- Smolen, P., Hardin, P. E., Lo, B. S., Baxter, D. A. & Byrne, J. H. (2004) *Biophys. J.* **86**, 2786–2802.
- Smolen, P., Baxter, D. A. & Byrne, J. H. (2003) *OMICS* **7**, 337–354.
- Tyson, J. J., Hong, C. I., Thron, C. D. & Novak, B. (1999) *Biophys. J.* **77**, 2411–2417.
- Winfree, A. T. (1980) *The Geometry of Biological Time* (Springer, New York).
- Gonze, D., Halloy, J. & Goldbeter, A. (2002) *Proc. Natl. Acad. Sci. USA* **99**, 673–678.
- Ruoff, P. (1992) *J. Interdiscipl. Cycle Res.* **23**, 92–99.
- Kurosawa, G. & Iwasa, Y. (2005) *J. Theor. Biol.* **233**, 453–468.
- Hong, C. I. & Tyson, J. J. (1997) *Chronobiol. Int.* **14**, 521–529.
- Leloup, J. C. & Goldbeter, A. (1997) *Chronobiol. Int.* **14**, 511–520.
- Ruoff, P., Vinsjevik, M. & Rensing, L. (2000) *Comments Theor. Biol.* **5**, 361–382.
- Ruoff, P., Rensing, L., Kommedal, R. & Mohsenzadeh, S. (1997) *Chronobiol. Int.* **14**, 499–510.
- Davis, R. H. (2000) *Neurospora, Contributions of a Model Organism* (Oxford Univ. Press, New York).
- Dunlap, J. C. & Loros, J. J. (2004) *J. Biol. Rhythms* **19**, 414–424.
- Loros, J. J. & Dunlap, J. C. (2001) *Annu. Rev. Physiol.* **63**, 757–794.
- Froehlich, A. C., Pagueiro, A., Lee, K., Denault, D., Colot, H., Nowrousian, M., Loros, J. J. & Dunlap, J. C. (2003) *Novartis Found. Symp.* **253**, 184–198; discussion 102–109, 198–202, 281–284.
- Goodwin, B. C. (1965) *Adv. Enzyme Regul.* **3**, 425–438.
- Ruoff, P. & Rensing, L. (1996) *J. Theor. Biol.* **179**, 275–285.
- Ruoff, P., Vinsjevik, M., Monnerjahn, C. & Rensing, L. (1999) *J. Biol. Rhythms* **14**, 469–479.
- Ruoff, P., Mohsenzadeh, S. & Rensing, L. (1996) *Naturwissenschaften* **83**, 514–517.
- Liu, Y., Loros, J. & Dunlap, J. C. (2000) *Proc. Natl. Acad. Sci. USA* **97**, 234–239.
- Gorl, M., Merrow, M., Huttner, B., Johnson, J., Roenneberg, T. & Brunner, M. (2001) *EMBO J.* **20**, 7074–7084.
- Noyes, R. M. (1986) in *Investigations of Rates and Mechanisms of Reactions*, Techniques of Chemistry, ed. Bernasconi, F. (Wiley, New York), 4th Ed., Vol. 6, pp. 373–423.
- Laidler, K. J. & Meiser, J. H. (1995) *Physical Chemistry* (Houghton Mifflin, Geneva, IL), 2nd Ed.
- Heinrich, R. & Schuster, S. (1996) *The Regulation of Cellular Systems* (Chapman & Hall, New York).
- Kacser, H. & Burns, J. A. (1973) *Symp. Soc. Exp. Biol.* **27**, 65–104.
- Hastings, J. W. & Sweeney, B. M. (1957) *Proc. Natl. Acad. Sci. USA* **43**, 804–811.
- Franck, U. F. (1980) *Ber. Bunsenges Phys. Chem.* **84**, 334–341.
- Radhakrishnan, K. & Hindmarsh, A. C. (1993) *Description and Use of LSODE, the Livermore Solver for Ordinary Differential Equations* (NASA Reference Publication 1327, Lawrence Livermore National Laboratory Report UCRL-ID-113855).
- Ruoff, P., Behzadi, A., Hauglid, M., Vinsjevik, M. & Havas, H. (2000) *Chronobiol. Int.* **17**, 733–750.
- Lee, K., Loros, J. J. & Dunlap, J. C. (2000) *Science* **289**, 107–110.
- Crosthwaite, S. K., Loros, J. J. & Dunlap, J. C. (1995) *Cell* **81**, 1003–1012.
- Crosthwaite, S. K., Dunlap, J. C. & Loros, J. J. (1997) *Science* **276**, 763–769.
- He, Q., Cheng, P., Yang, Y., Yu, H. & Liu, Y. (2003) *EMBO J.* **22**, 4421–4430.
- Liu, Y., Merrow, M., Loros, J. J. & Dunlap, J. C. (1998) *Science* **281**, 825–829.
- Gardner, G. F. & Feldman, J. F. (1981) *Plant Physiol.* **68**, 1244–1248.
- Yang, Y., He, Q., Cheng, P., Wraga, P., Yarden, O. & Liu, Y. (2004) *Genes Dev.* **18**, 255–260.
- Yang, Y., Cheng, P., He, Q., Wang, L. & Liu, Y. (2003) *Mol. Cell. Biol.* **23**, 6221–6228.
- Yang, Y., Cheng, P. & Liu, Y. (2002) *Genes Dev.* **16**, 994–1006.
- Yang, Y., Cheng, P., Zhi, G. & Liu, Y. (2001) *J. Biol. Chem.* **276**, 41064–41072.
- He, Q., Cheng, P. & Liu, Y. (2005) *Genes Dev.* **19**, 1518–1531.
- Field, R. J., Körös, E. & Noyes, R. M. (1972) *J. Am. Chem. Soc.* **94**, 8649–8664.
- Ruoff, P. (1995) *Physica. D* **84**, 204–211.