We have the following two expressions for the rate q,

$$q = \frac{k}{\mu} A \frac{\rho g(h(t) - h_b)}{\Delta l 1.01325 \cdot 10^6}$$

for the rate through the core with water level difference $(h(t) - h_b)$ between inlet and outlet end, and

$$q = -\frac{\mathrm{d}h}{\mathrm{d}t}A_r,$$

for the discharge of the water in the cylinder. These two expressions for q are set equal. The result is a first order differential equation for h as a function of t. One has to use that $\int dh/h = \ln h$. Applying the initial condition that $h = h_0$ when t = 0, we find the expression given.

In SI-units (ρgh) is in (kg/m³· m/s²· m) which is kg/(m s²) which again is N/m² or Pa. If we use (ρgh) in g/(cm s²) we get a factor 10 in difference, i.e., (ρgh) in the given units is equal to 1013250 atmospheres.

By plotting the left-hand-side of the equation against time t, the permeability may be calculated from the slope of the resulting straight line.